

HEC-RAS 2D: Sediment Transport Theory

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Outline




- Sediment Particles
- Bulk Bed Properties
- Incipient Motion
- Erosion/Entrainment and Deposition/Settling
- Sediment Transport Modes
- Sediment Transport Functions
 - How much sediment is transported?
- Transport Processes: Advection and diffusion
- Bed Sorting and Layering


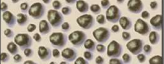






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Sediment Particles



A. Grain size		B. Rounding		
"Gravel" > 2mm	Pebbles 4–64 mm 	Angular	Sub-rounded	Well-rounded
	Granules 2–4 mm 	C. Sorting		
	Coarse sand 0.5–2 mm 	Poorly sorted		
	Medium sand 0.25–0.5 mm 	Well-sorted		
	Fine sand 0.06–0.25 mm 	D. Grains and matrix		
	Silt 0.004–0.06 mm 			
	Clay < 0.004 mm 			

Diameter types

- Sieve diameter (most common)
- Settling diameter
- Nominal diameter



Density


$$\rho_s = \frac{\text{particle mass}}{\text{particle volume}}$$

Shape


Roundness

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Sediment Bed Material



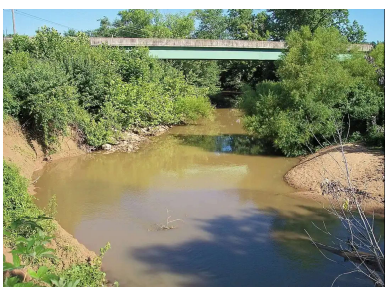
- Natural rivers have a distribution of size classes with different shapes, densities, etc.



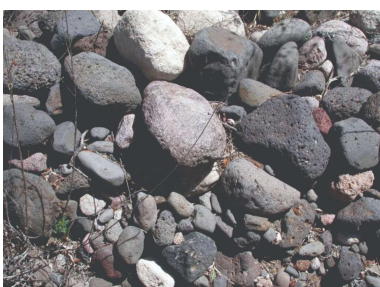
Sand



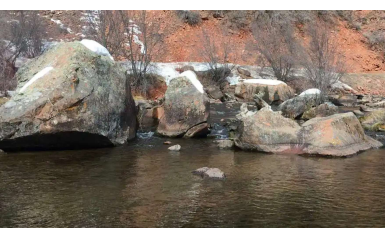
Gravel



Mud




Cobble




Boulders

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Sediment Bed Bulk Properties



- Porosity

$$\phi = \frac{\text{volume of voids}}{\text{total volume}}$$

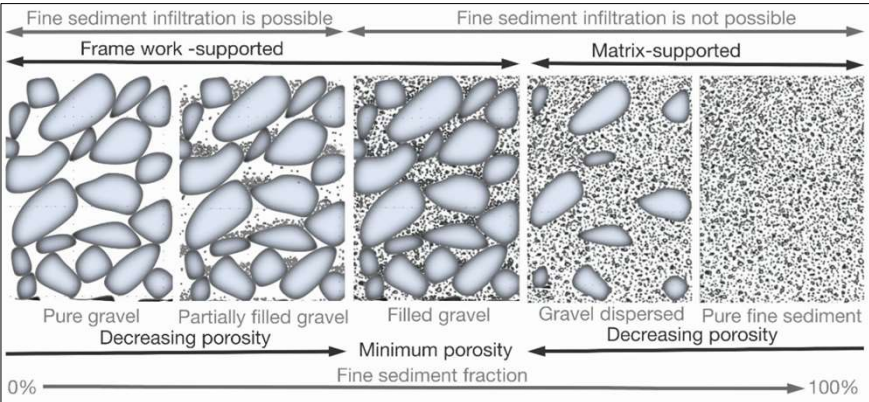
- Solidity

$$1 - \phi = \frac{\text{volume of solids}}{\text{total volume}}$$

- Dry density


$$\rho_d = \frac{\text{mass}}{\text{total volume}}$$

(bed mass concentration)




Bui, V.H.; Bui, M.D.; Rutschmann, P. Advanced Numerical Modeling of Sediment Transport in Gravel-Bed Rivers. *Water* 2019, 11, 550. <https://doi.org/10.3390/w11030550>

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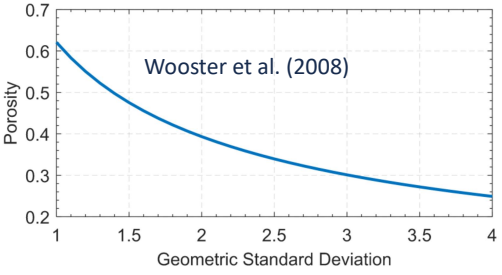
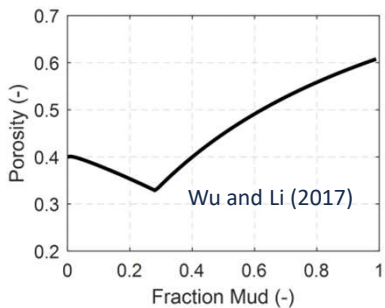


Sediment Bed Porosity




In HEC-RAS, for newly deposited sediments


- Porosity
 - Noncohesive fraction computed with Colby formula as a function of the "grain porosities" or the Wooster et al. (2008)
 - Cohesive fraction computed with Colby formula
- Packing is only considered for mixed (cohesive and noncohesive sediments) using the Wu and Li (2017)

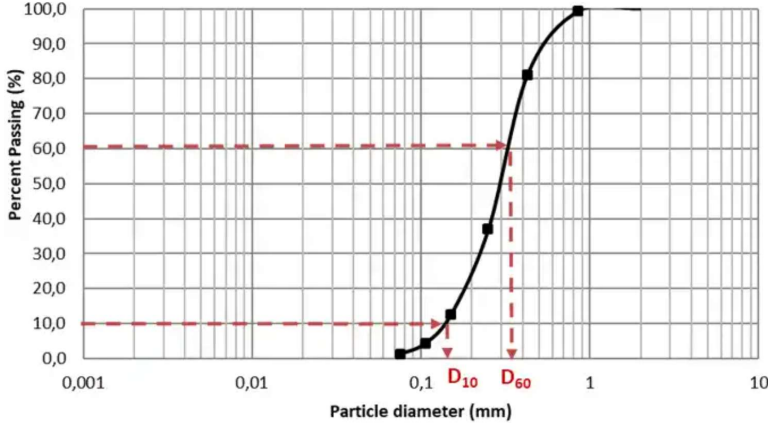
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Grain Size Distribution




- Diameters
 - Geometric mean
 - Percentile diameters
 - D_p
 where P is percent finer
 - D_{50} : Median grain size
- Sorting
 - Standard deviation
 - Lower is more sorted
- Skewness
 - Symmetry of curve
 - Lower is more symmetric
- Kurtosis
 - “Peakedness” of curve

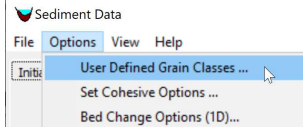


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Grain Classes



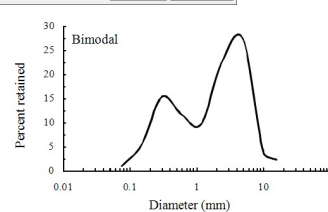
Class	Label	Min	Max	Mean	SG	n	UW	Coh?	De
1	Clay	0.002	0.004	0.003	2.65	0.82	30	1	1
2	VPM	0.004	0.008	0.006	2.65	0.61	65	1	1
3	M	0.008	0.016	0.011	2.65	0.61	65	1	1
4	MM	0.016	0.032	0.023	2.65	0.61	65	1	1
5	CM	0.032	0.0625	0.045	2.65	0.61	65	1	1
6	VFS	0.0625	0.125	0.088	2.65	0.44	93	0	1
7	FS	0.125	0.25	0.177	2.65	0.44	93	0	0.4
8	MS	0.25	0.5	0.354	2.65	0.44	93	0	0.09
9	CS	0.5	1	0.707	2.65	0.44	93	0	0.09
10	VCS	1	2	1.41	2.65	0.44	93	0	0.09
11	MG	2	4	2.83	2.65	0.44	93	0	0.09
12	FG	4	8	5.66	2.65	0.44	93	0	0.09
13	MG	8	16	11.3	2.65	0.44	93	0	0.09
14	CG	16	32	22.6	2.65	0.44	93	0	0.09
15	VCG	32	64	45.3	2.65	0.44	93	0	0.09
16	SC	64	128	90.5	2.65	0.44	93	0	0.09
17	LC	128	256	181	2.65	0.44	93	0	0.09
18	SB	256	512	362	2.65	0.44	93	0	0.09
19	MB	512	1024	724	2.65	0.44	93	0	0.09
20	LB	1024	2048	1448	2.65	0.44	93	0	0.09

Currently Default:

Density Method: Unit Weight (All Classes)

Enforce Adjacent-Non-Overlapping Grain Classes and Geometric Mean

OK Cancel



- Continuous grain size distribution discretized into bins or grain classes
- Select grain classes carefully and only use them when necessary
 - Do not add a grain class which represents 0.1% of the bed material
 - Each grain class adds a transport equation, bed change, and sorting equation
- Active grain classes detected from initial bed gradations and boundary conditions

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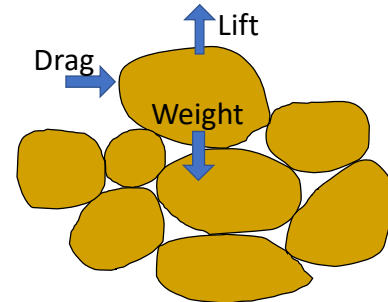
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Incipient Motion of Noncohesive Beds



- Usually defined as a threshold/critical shear or velocity which produces transport
- Sometimes defined as a threshold (non-dimensional) transport rate
- Depends on particle shape, density, random arrangement of particles, and many other forces



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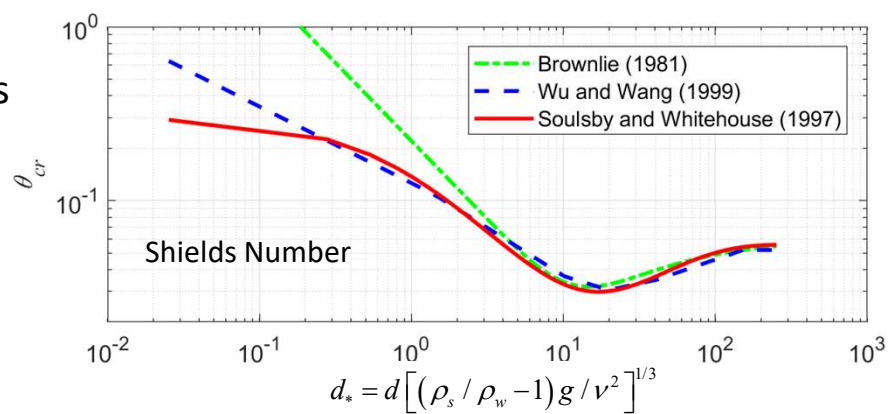


Critical Shear for Noncohesives



Shields Number is a ratio of forces

$$\theta_{cr} = \frac{\tau_{cr}}{(\rho_s - \rho_w)gd}$$



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Hiding and Exposure



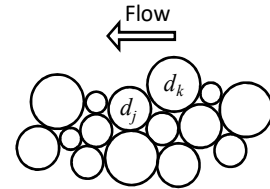
- Smaller particles “hidden” from flow and larger particles “exposed” to flow
- Hiding and exposure corrections

- Incipient motion/mobility

$$\xi_k = \frac{\theta_{crk}}{\theta_{cr}} = \frac{\tau_{crk}}{\tau_{cr}} = \frac{U_{crk}^2}{U_{cr}^2}$$

- Transport

$$\eta_k = \frac{q_k^*}{q^*} \quad \eta_k \approx \frac{1}{\xi_k^a} \quad a: \text{Coefficient}$$



- Correction on incipient motion done whenever possible unless formula does not have a threshold for incipient motion
- Because finer grain sizes represent a larger portion of the transported material, **applying** hiding/exposure corrections will generally **reduce** the overall transport

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Hiding and Exposure Functions




- HEC-RAS has several options for the hiding and exposure correction
 - Ashida and Michiue (1971)
 - Day (1980)
 - Developed for Ackers and White formula
 - Egiazaroff (1965)
 - Used in AdH
 - Parker et al. (1982)
 - Hayashi (1980)
 - Proffitt and Sutherland (1983)
 - Developed for Ackers and White
 - Wilcock and Crowe
 - Wu et al. (2000)

Notes:


- **ALWAYS** use hiding and exposure corrections (default is off)
- Formulation and exponent can be calibrated using bed gradations or fractional suspended concentrations

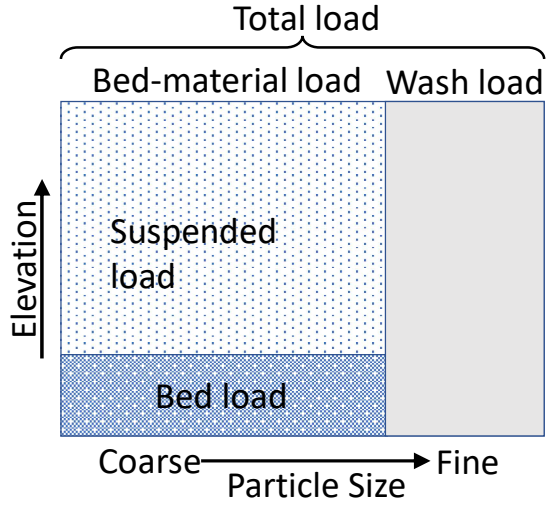
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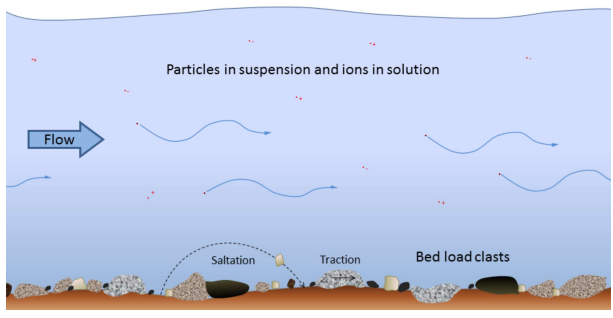
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Sediment Loads









- Wash load does not contribute to the bed.
- HEC-RAS simulate the total load
- Bed load particles move by sliding/traction, saltation/jumping, and rolling
- Suspended sediments are entrained in the water column through vertical mixing

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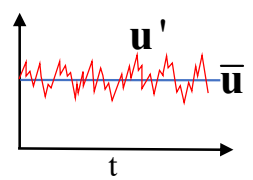
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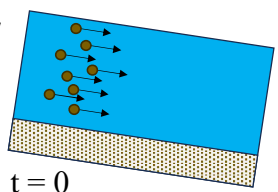
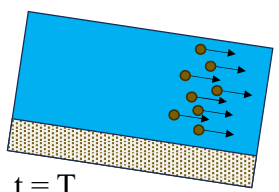
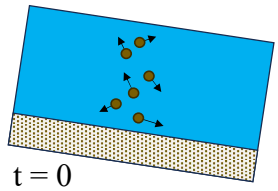
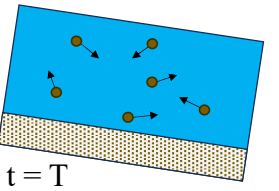
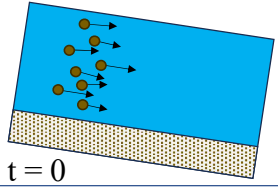
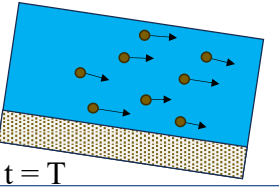


Transport Processes



- Fluid/particle velocity
 $\mathbf{u} = \bar{\mathbf{u}} + \mathbf{u}'$
- Mean velocity
 $\bar{\mathbf{u}}$
- Turbulent velocity
 $\mathbf{u}' \quad \overline{\mathbf{u}'} = 0$



<p>Advection only</p> <p>$\bar{\mathbf{u}} \neq 0$</p> <p>$\mathbf{u}' = 0$</p>	 $t = 0$	 $t = T$
<p>Diffusion only</p> <p>$\bar{\mathbf{u}} = 0$</p> <p>$\mathbf{u}' \neq 0$</p>	 $t = 0$	 $t = T$
<p>Advection and Diffusion</p> <p>$\bar{\mathbf{u}} \neq 0$</p> <p>$\mathbf{u}' \neq 0$</p>	 $t = 0$	 $t = T$

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Erosion and Deposition



- Erosion defined as any removal of bed material
 - Can be bed load or suspended load
- Entrainment is the suspension of bed material into the water column due to vertical mixing
- Settling is the downward velocity of particles in the water column due to gravity
- Deposition defined as the addition of any material to the bed
 - Can be from bed load or suspended load
 - i.e. settling at the bed
- Wash load does not interact with the bed

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Erosion



- Physics based formulas for erosion due not exist
- Various empirical and semi-empirical methods exist
- Suspended load sediment modeling
 - Near-bed gradient (Neumann) boundary condition
 - Utilizes a near-bed concentration capacity which can be difficult to estimate
 - Does not require any other parameters
 - Adaptation approach
 - Utilizes an equilibrium transport rate which easier to estimate but
 - Requires an adaptation parameter which can be hard to estimate
- Bed load sediment modeling
 - Most commonly uses an adaptation approach
- Details of adaptation approach discussed later

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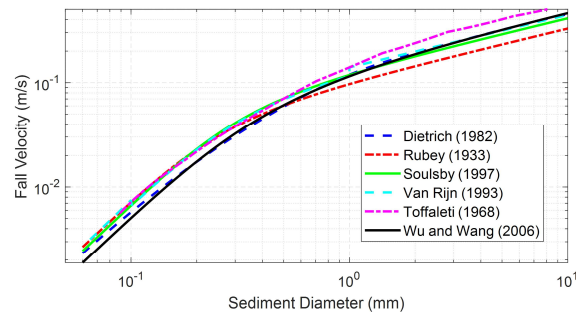
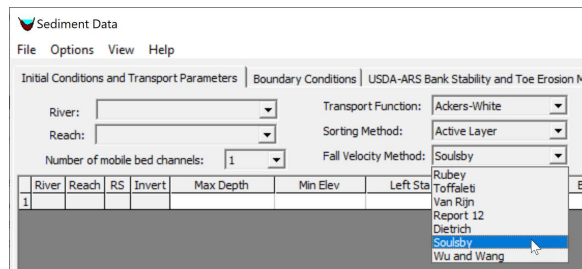
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Deposition



- Fall velocity method represents free settling velocity
 - Does not account for hindered settling or flocculation
- Not a calibration parameter
- Use Soulsby except for specific conditions



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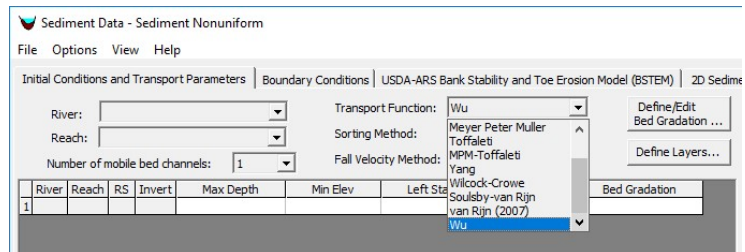
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Transport Functions



- Represent equilibrium sediment transport under uniform steady conditions
- Most important model setting
- Available formulas
 - Ackers and White (1973)
 - Engelund-Hansen (1967)
 - Lausen-Copeland (1989)
 - Meyer-Peter-Muller (1948)
 - Soulsby-van Rijn (1997)
 - Toffaleti (1968)
 - Van Rijn (1984ab, 2007ab)
 - Wilcock and Crowe (2003)
 - Wu et al. (2000)
 - Yang (1984)



- Most common for 2D are:
 - Soulsby van Rijn
 - Van Rijn
 - Wu

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Ackers and White (1973)



- Total-load Formula
- Excess mobility based on stream power
- Fractional load formulation adopted for nonuniform sediments by Day (1980) and Proffitt and Sutherland (1983) for nonuniform sediments
- Works well for nonuniform sands and gravels

$$q_{tk}^* = \rho_w g h U X_{tk}^* \quad \frac{X_{tk}^* h \rho_w}{d_k \rho_{sk}} \left(\frac{u_*}{U} \right)^n = \Lambda \left(\frac{F_{grk}}{A_c} - 1 \right)^m$$

$$F_{grk} = \eta_k \frac{u_*^n}{\sqrt{R_k g d_k}} \left[\frac{U}{\sqrt{32 \log_{10}(10h/d_k)}} \right]^{1-n} \quad R_k = \rho_{sk} / \rho_w - 1$$

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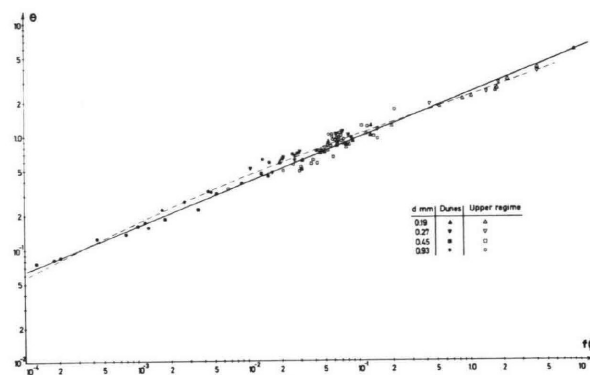
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Engelund-Hansen (1967)



- Total-load Formula
- Threshold for transport
 - Originally did not use one
 - Included in HEC-RAS 2D Sediment
- Uniform sediments dominated by suspended load



$$q_{tk}^* = \begin{cases} 0.05 \eta_k \rho_{sk} U^2 \sqrt{\frac{d_k}{g R_k}} \left(\frac{\tau_b}{g(\rho_{sk} - \rho_w) d_k} \right)^{3/2} & \text{for } \tau_b > \tau_{crk} \\ 0 & \text{otherwise} \end{cases}$$

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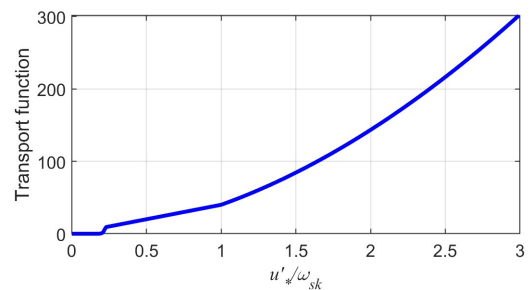


Laursen-Copeland (1968, 1989)



- Total-load Formulas
- Nonlinear excess shear formulation with empirical transport function
- Based on flume experiments and data from Arkansas River
- Copeland extended Laursen equation to gravel

$$q_{ik}^* = a \rho_w U h \left(\frac{d_k}{h} \right)^{7/6} \left(\frac{\theta'_b}{\theta_{crk}} - 1 \right)^n f_{ik}^{LC} \left(\frac{u'_*}{\omega_{sk}} \right)$$



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Meyer-Peter-Müller (1948)



- Bed-load Formula
- Excess shear formulation
- Recalibrated several times in literature
- Most appropriate for uniform gravel
- Tends to under-predict for sands and silts

$$q_{bk}^* = A_M \rho_{sk} \sqrt{R_k g d_k^3} (\theta'_b - \theta_{crk})^{E_M}$$

$$MPM \Rightarrow A_M = 8, E_M = 2/3, \text{ and } \theta_{crk} = 0.047$$

$$\text{Wong and Parker (2006)} \Rightarrow A_M = 3.97, E_M = 1.6, \text{ and } \theta_{crk} = 0.0495$$

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Soulsby-van Rijn (1997)



- Total-load Formulas
- Developed by curve-fitting to a 2DV sediment transport model SEDTRANS by van Rijn
- Uses depth-averaged threshold current velocity
- Originally proposed for well sorted sands and extended here for nonuniformly sized sediments

$$q_{bk}^* = 0.005Uh \left(\frac{U - U_{crk}}{\sqrt{R_k g d_k}} \right)^{2.4} \left(\frac{d_k}{h} \right)^{1.2}$$

$$q_{sk}^* = 0.012Uh \left(\frac{U - U_{crk}}{\sqrt{R_k g d_k}} \right)^{2.4} \left(\frac{d_k}{h} \right) d_{*k}^{-0.6}$$

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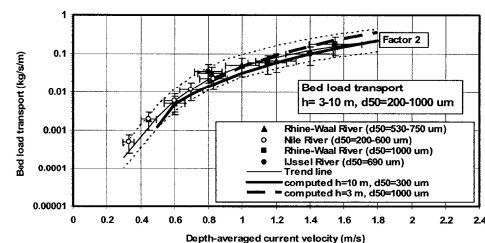
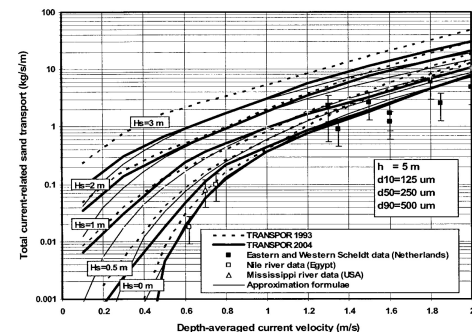
Van Rijn (1984ab, 2007ab)



- Total-load Formula
- Developed by curve-fitting to lab and field measurements
- Uses depth-averaged threshold current velocity
- Originally proposed for well sorted sands and extended here for nonuniformly sized sediments
- Suspended-load formula the same as the Soulsby-van Rijn

$$q_{bk}^* = 0.015Uh \left(\frac{U - U_{crk}}{\sqrt{R_k g d_k}} \right)^{1.5} \left(\frac{d_k}{h} \right)^{1.2}$$

$$q_{sk}^* = 0.012Uh \left(\frac{U - U_{crk}}{\sqrt{R_k g d_k}} \right)^{2.4} \left(\frac{d_k}{h} \right) d_{*k}^{-0.6}$$



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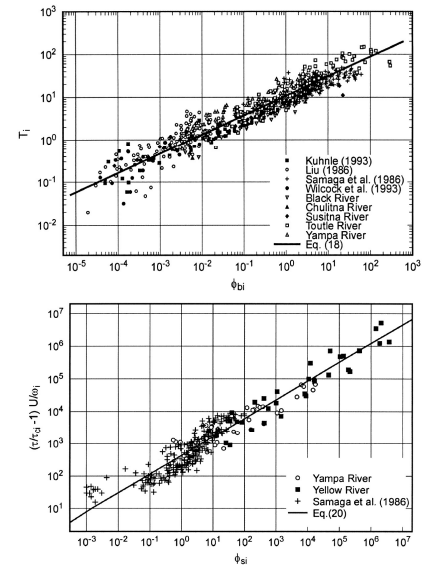


Wu et al. (2000)

- Total-load Formula
- Developed for nonuniform sediments
- Based on extensive lab and field measurements
- Nonlinear excess shear formulation for bed-load
- Stream-power formulation for suspended-load

$$q_{bk}^* = 0.0053 \sqrt{R_k g d_k^3} \left(\frac{\tau_b'}{\tau_{crk}} - 1 \right)^{2.2}$$

$$q_{sk}^* = 2.62 \times 10^{-5} \sqrt{R_k g d_k^3} \left[\left(\frac{\tau_b}{\tau_{crk}} - 1 \right) \frac{U}{\omega_{sk}} \right]^{1.74}$$



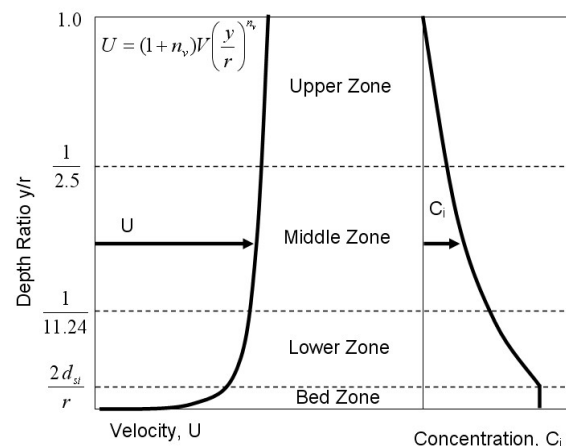
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Toffaletti (1968)

- Total-load formulas
- Developed primarily for sand
- Splits the water column into 3 zones
- Assumes Rouse concentration profile
- Originally developed for bulk transport but here it is applied to individual grain classes
- Usually applied at “large” rivers since most of the data used to develop it were from large suspended-load dominant rivers
- Bed-load formula does not perform well for gravel and can be replaced with MPM



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Wilcock and Crowe (2003)



- Bed-load Formula
- Developed for graded beds with sand and gravel
- No critical shear for transport
- However, it quickly goes to zero

$$q_{bk}^* = \frac{u_*^3 W_k^*}{R_k g}$$

$$W_k^* = \begin{cases} 0.002\phi^{7.5} & \text{for } \phi < 1.35 \\ 14 \left(1 - \frac{0.894}{\phi^{0.5}} \right)^{4.5} & \text{for } \phi \geq 1.35 \end{cases} \quad \phi = \frac{\tau_b}{\tau_{r,k}}$$

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Yang (1979, 1984)




- Total-load formula
- Regression of potential energy dissipation
- Best for fine to medium sands
- Overestimates for coarse sands and gravel
- Sharp discontinuity at diameter of 2 mm

$$\log_{10}(C_{tk}^*) = M + N \log_{10} \left[\frac{S_f}{\omega_{sk}} (U - U_{crk}) \right]$$


$$M = M \left(\frac{\omega_{sk} d_k}{\nu}, \frac{u_*}{\omega_{sk}} \right), \quad N = N \left(\frac{\omega_{sk} d_k}{\nu}, \frac{u_*}{\omega_{sk}} \right)$$

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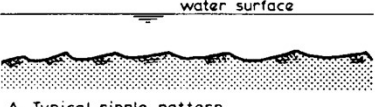


Bed Forms and Roughness

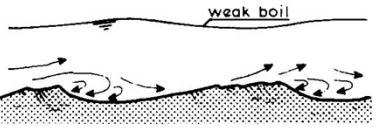


- Total Roughness sum of
 - Bed form
 - Grain/skin
 - Transport (usually ignored)

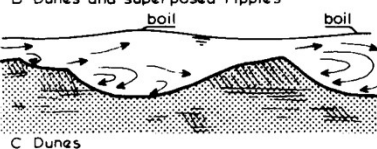
$$k_s = k_{s,f} + k_{s,g} + k_{s,s}$$



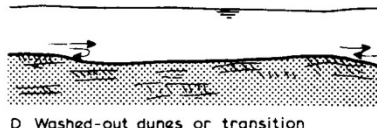
A Typical ripple pattern



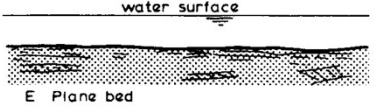
B Dunes and superposed ripples




C Dunes



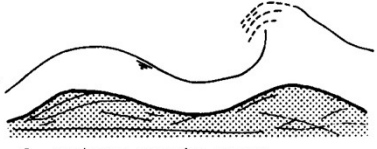
D Washed-out dunes or transition



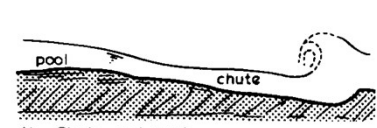
E Plane bed



F Antidune standing waves




G Antidune breaking waves




H Chute and pool

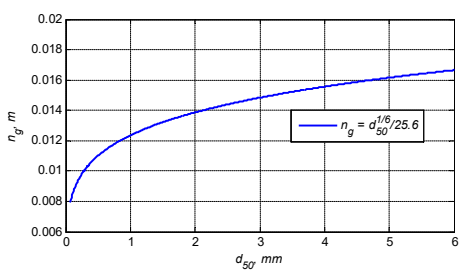
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Bed Roughness and Bed Shear

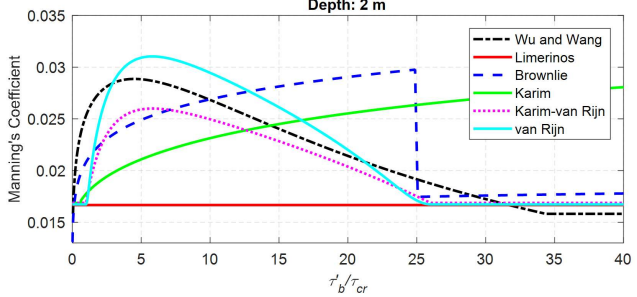


- Total Roughness sum of
 - Bed form
 - Grain/skin
 - Transport (usually ignored)
- Bed shear decomposed into total shear and grain shear
- Suspended load generally a function of total shear
- Bed load a function of grain shear

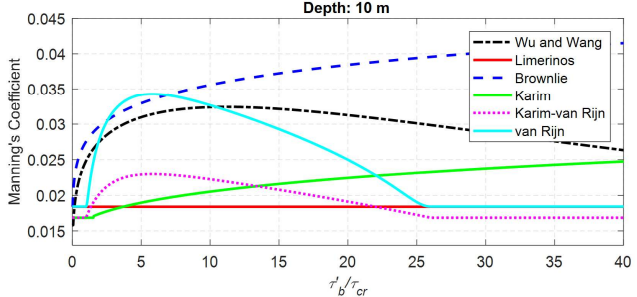


$n_g = d_{50}^{1/6} / 25.6$

Depth: 2 m



Depth: 10 m



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Equilibrium vs Non-Equilibrium Transport



- Equilibrium
 - Actual transport rate = equilibrium transport rate
 - No under-loading or over-loading which is when the actual transport is less or more than the equilibrium transport rate
 - Assumes steady and uniform flow and sediment conditions
- Non-equilibrium
 - Actual transport rate \neq equilibrium transport rate
 - Can have under- or over-loading
 - Applicable to unsteady and nonuniform flow and sediment conditions

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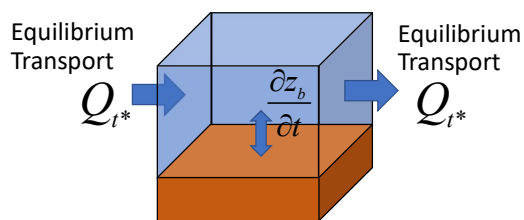
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Equilibrium vs Non-Equilibrium Modeling

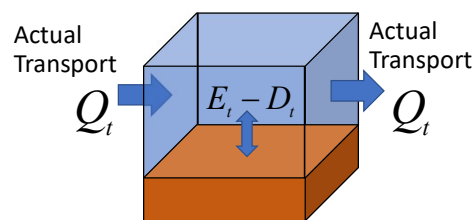


Equilibrium Modeling Approach



1. Compute inward and outward equilibrium transport rates
2. Bed change is mass balance in control volume

Non-Equilibrium Modeling Approach



1. Solve transport equation(s) for actual concentrations
 - Erosion from empirical formulas
 - Deposition from actual concentration
2. Bed change from erosion and deposition

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Deriving Exner



- Starting with the transport and bed change equations while ignoring the temporal and diffusion terms

$$\cancel{\frac{\partial(hC_t)}{\partial t}} + \frac{\partial(hUC_t)}{\partial x} = \frac{\partial}{\partial x} \left(\cancel{\epsilon_t h} \frac{\partial C_t}{\partial x} \right) + E_t - D_t \quad \rho_s (1 - \phi_b) \frac{\partial z_b}{\partial t} = D_t - E_t$$

- Assuming the concentration is at equilibrium and defining the transport rate

$$C_t = C_{t^*} = \frac{Q_{t^*}}{hU}$$

- Combining the equations leads to the Exner equation

$$\rho_s (1 - \phi_b) \frac{\partial z_b}{\partial t} + \frac{\partial Q_{t^*}}{\partial x} = 0$$

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Equilibrium vs. Non-Equilibrium Transport



Equilibrium

- Pros
 - Simpler
 - Computationally efficient
 - Less parameters
 - Works well for large-scale models
- Cons
 - Less realistic
 - Breaks down for high-resolution models

Non-Equilibrium

- Pros
 - Physically-based
 - Works for all scales
- Cons
 - Computationally expensive
 - More parameters to calibrate

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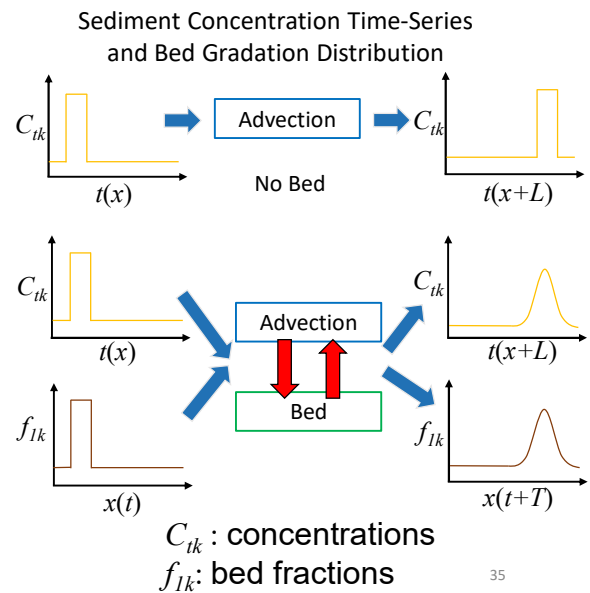
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Dispersion from Bed Mixing



- Most natural conditions are **advection-dominated**
- Diffusion is utilized here to describe the horizontal mixing of sediment **in the water column** due to turbulent mixing and dispersion
- **Dispersion** of bed material also occurs due to the bed mixing
 - Bed provides a storage mechanism



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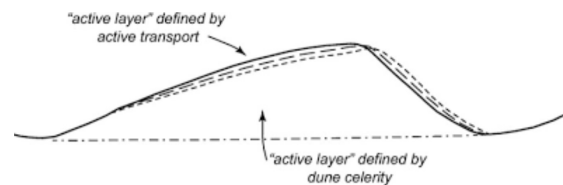
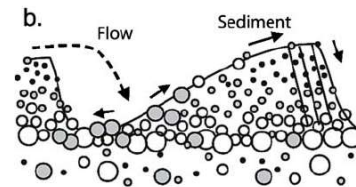


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Active Layer

- Top bed layer which exchanges material with transport
- Grain size, scale, and time dependent
- At modeling scales is at least half the bed form thickness
- Active layer should be thicker for very dynamic models or models with coarse grids and large time steps



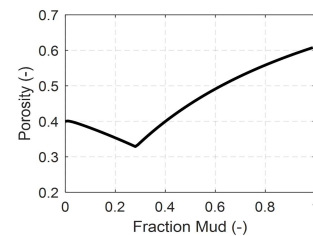
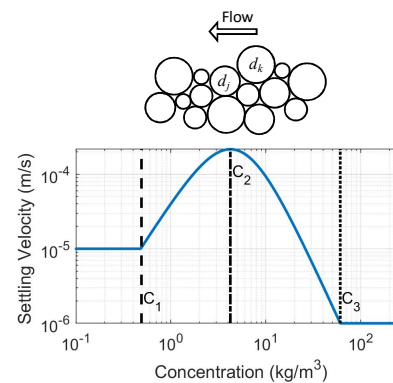
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HEC-RAS 2D Sediment

- Key Features
 - Mixed cohesive and non-cohesive
 - Variable particle and bed bulk density
 - Quasi-3D effects
 - Hiding and exposure corrections
 - Bed-slope effects
 - Bed roughness predictors
 - Packing model for bed porosity
 - Avalanching
 - Hindered settling
 - Flocculation $f(C, T)$
 - Consolidation
 - Vertically varying cohesive properties
 - Sheet and splash erosion
 - Morphologic Acceleration
 - **Subgrid bathymetry, bed sorting, erosion, deposition, and hydrodynamics**




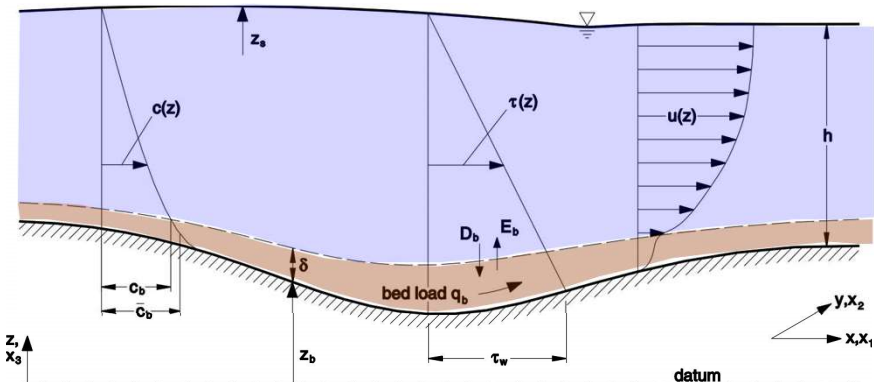
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Sediment Model Definitions





Volumetric Bed-load transport:


Suspended-load transport:

$$q_b = C_b u_b \delta_b$$


C_b = volumetric concentration in the bed-load layer
 u_b = particle velocity (m/s)
 δ_b = thickness of bed-load layer (m)

$$q_s = \int_{\delta_b}^h u c dz$$

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Concentration Definition



- **Depth-averaged**

$$\hat{C}_{tk} = \frac{1}{h} \int_0^h c_{tk} dz$$

$$q_{tk} = \beta_t U h \hat{C}_{tk}$$

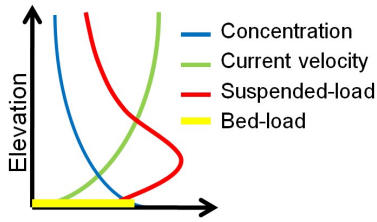
$$\beta_t = \frac{1}{U h \hat{C}_{tk}} \int_0^h u c_{tk} dz$$

- Coefficient for transport (advection term)
- **Used in HEC-RAS 1D**
- **Velocity weighted (Einstein definition)**

$$C_{tk} = \frac{1}{U h} \int_0^h u c_{tk} dz$$


$$q_{tk} = U h C_{tk}$$

- Simpler formula for transport (advection term)
- **Used in HEC-RAS 2D**
- Coefficient in temporal term




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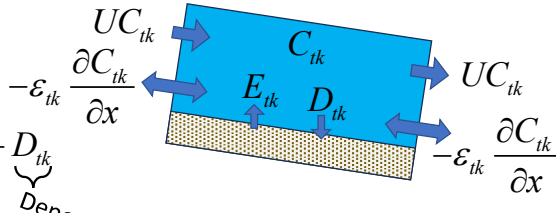


Total-load Transport Equation



- Unsteady Advection-Diffusion Equation

$$\underbrace{\frac{\partial}{\partial t} \left(\frac{hC_{tk}}{\beta_{tk}} \right)}_{\text{Temporal or Storage}} + \underbrace{\nabla \cdot (hUC_{tk})}_{\text{Advection}} = \underbrace{\nabla \cdot (\epsilon_{tk} h \nabla C_{tk})}_{\text{Diffusion}} + \underbrace{E_{tk}}_{\text{Erosion}} - \underbrace{D_{tk}}_{\text{Deposition}}$$



k : Grain class

h : Water depth

C_{tk} : Total-load concentration

β_{tk} : Total-load correction factor

U : Current velocity

ϵ_{tk} : Total-load diffusion coefficient


E_{tk} : Total-load erosion rate

D_{tk} : Total-load deposition rate


- Simulating total-load instead of separate bed- and suspended-loads reduces computational costs because it requires half as many transport equations

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Load Correction Factor



- Accounts for vertical shape of concentration and velocity profiles
- Represents the reduction in sediment transport velocity and delay in sediment response
- Total-load correction factor

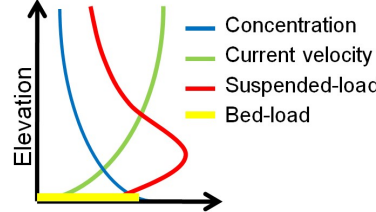
$$\beta_{tk} = \frac{1}{r_{sk} / \beta_{sk} + (1 - r_{sk}) / \beta_{bk}}$$

- Suspended load correction factor

$$\beta_{sk} = \frac{1}{UhC_{tk}} \int_0^h uc_k dz$$

- Bed load correction factor

$$\beta_{sk} = \frac{u_{bk}}{U}$$



$r_{sk} = \frac{q_{sk}}{q_{tk}}$

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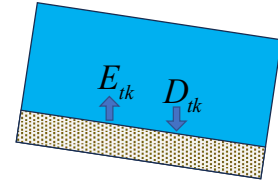


Bed Change



- Fractional Bed Change

$$\underbrace{\rho_{sk}(1-\phi_b)}_{\text{Bed change}} \frac{\partial z_{bk}}{\partial t} = \underbrace{D_{tk}}_{\text{Deposition}} - \underbrace{E_{tk}}_{\text{Erosion}} + \underbrace{\nabla \cdot (\kappa_{bk} |q_{bk}| \nabla z_b)}_{\text{Bed slope term}}$$



- Total Bed Change

$$\frac{\partial z_b}{\partial t} = \sum_k \frac{\partial z_{bk}}{\partial t}$$

z_b : Bed elevation [L]

ρ_{sk} : Grain density [M/L³]

ϕ_b : Bed Porosity [-]

D_{tk} : Fractional deposition rate [M/L²/T]

E_{tk} : Fractional erosion rate [M/L²/T]

κ_{bk} : Bedslope coefficient [-]

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Bed Slope Coefficient

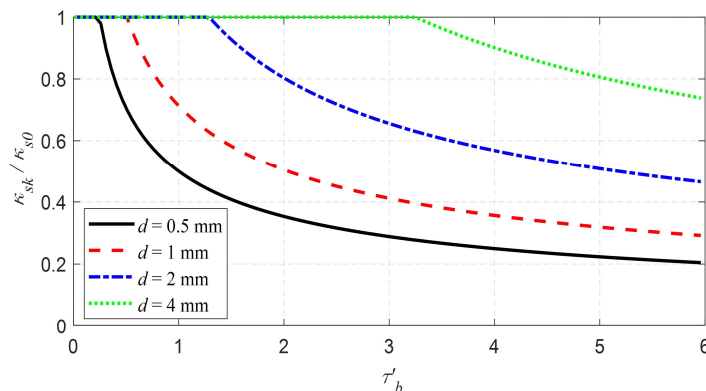


- Accounts for down-slope movement of sediment during transport
- Larger grains more influenced by bed-slope
- Bed-slope effect less with increasing transport
- Tends to smooth bed elevations and thereby improve stability

$$\kappa_{bk} = \kappa_{b0} \sqrt{\frac{\tau_{crk0}}{\max(\tau'_b, \tau_{crk0})}}$$


$$\kappa_{b0} \approx 0.1 - 0.5$$

$$\nabla \cdot (\kappa_{bk} |q_{bk}| \nabla z_b)$$




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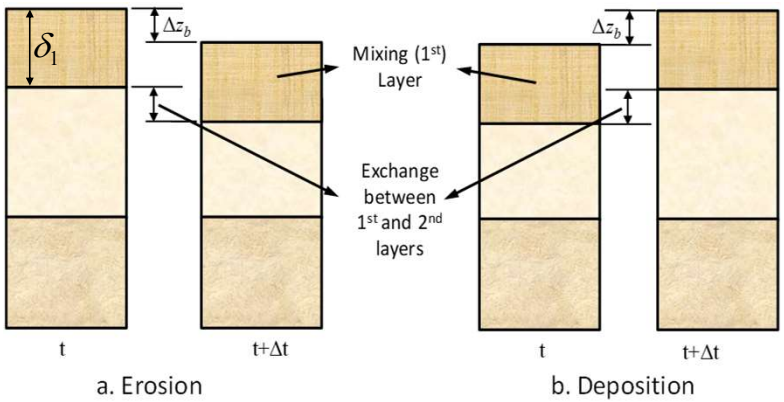
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Bed Sorting and Layering



- Bed divided into discrete layers
- Each layer has a bed gradation
- Top layer referred to as the active layer
- Active layer exchanges material with transport
- Exchange between first and second layers




$$\delta_1 = \max(f_{1,90}d_{90}, 0.5\Delta, \delta_{1,\min})$$


Δ : Bedform height

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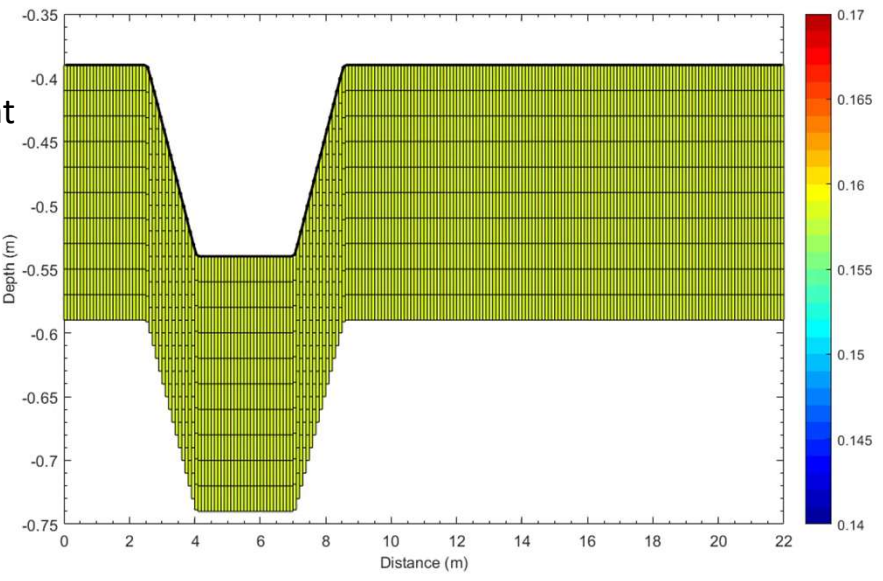


Bed Layering Example



- Flume experiment
- Flow from left to right
- 10 layers

Color Indicates Median Grain Size



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Notes on Bed Sorting Model



- Two types
 - ▶ Constant Bulk Density Model
 - ▶ Variable Bulk Density Model
- Automatically selected based on input input
- Constant bulk density model is simpler, faster, and more stable obviously because it has few

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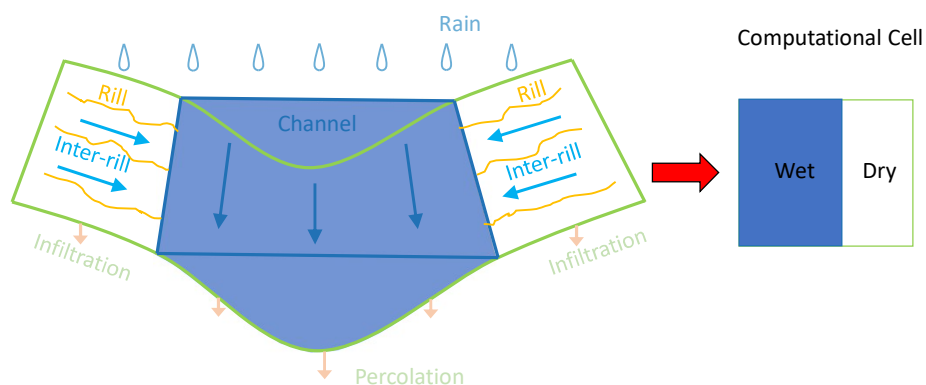
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Subgrid Modeling




- Representation of the physical terrain and processes at a subgrid scale
- Allows for larger grid cells reducing computational cells, and computational times




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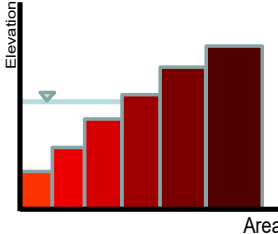
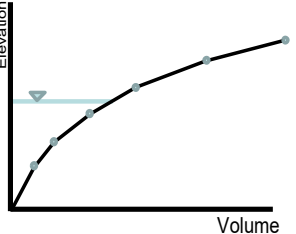
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Subgrid Modeling


Hydrodynamics








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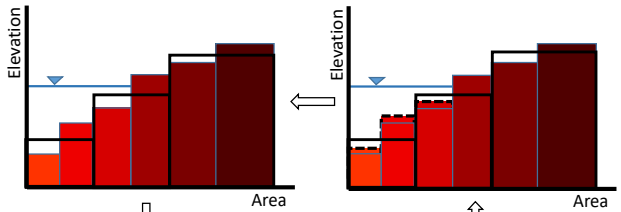
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Subgrid Modeling

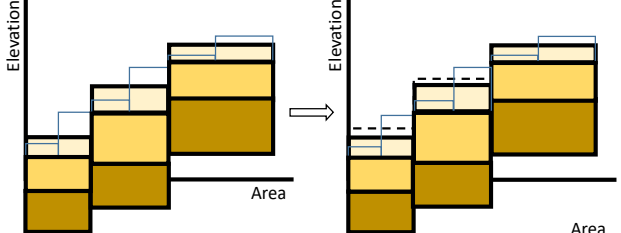


Flow





Sediment



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Shallow Water Eqs. vs. Diffusion Wave Eq.



- Use SWE for:
 - Flows with dynamic changes in acceleration
 - Studies with important wave effects, tidal flows
 - Detail solution of flows around obstacles, bridges or bends
 - Simulations influenced by Coriolis, mixing, or wind
 - To obtain high-resolution and detailed flows
- Use DWE for:
 - Flow is mainly driven by gravity and friction
 - Fluid acceleration is monotonic and smooth, no waves
 - To compute approximate global estimates such as flood extent
 - To assess approximate effects of dam breaks
 - To assess interior areas due to levee breaches
 - For quick estimations or preliminary runs

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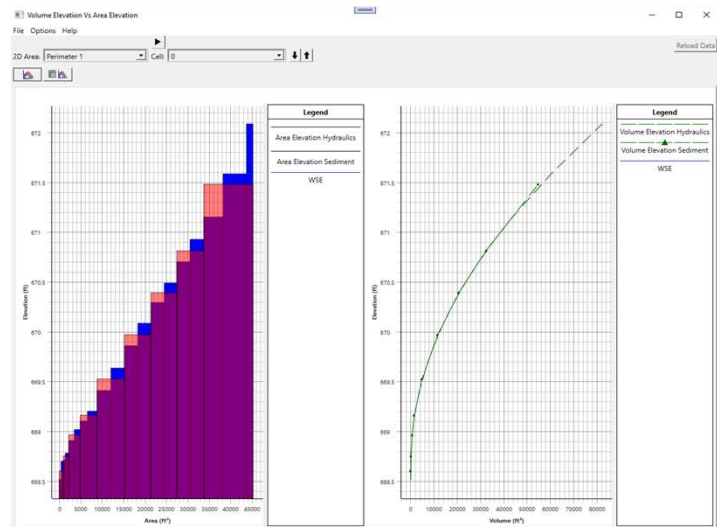
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Limitations



- Model initialization
- Terrain modification
- Coupling of 1D and 2D
- Dredging
- Secondary flow
- Particle infiltration/trapping



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Thank You!

HEC-RAS Website:

<https://www.hec.usace.army.mil/software/hecras/>

Online Documentation:

<https://www.hec.usace.army.mil/confluence/rasdocs>



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